

## OCCURRENCE OF THE DRY PERIODS IN EUROPEAN RUNOFF SERIES

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**Abstract:** Low flows of the Central European rivers in last years raised question if similar situation occurred also in the past or it indicates something extraordinary. The aim of the first part of the paper is to analyse the occurrence of the dry and wet periods in the Danube runoff series along the whole stream. The mean annual runoff from 7 stations along the Danube was taken for the analysis of the long-term variability of the annual flows. The most wet decade in Orsova was 1910–1919, and the driest one in 1857–1866. In the study some methods of the long-term trends identification in the hydrological time series are presented. Apart from the classical methods (like that of moving averages) the paper focuses in detail on the Hodrick-Prescott (HP) filter.

The dry periods of other 17 important European rivers are analysed in the second part of the paper. The annual discharge time series were recalculated to the standardised time series for three areas: territory of the West and Central Europe, territory of the East Europe and territory of North Europe. We used the Hodrick-Prescott (HP) filter for identification of the long-term trend of the standardized annual flows. The statistical analysis shows that in case of these series we can not observe long-term increase or decrease of the flows in last 150 years. We can identify only wet and dry periods of different duration. The extraordinary dry period occurred about the year 1863 as well as 86 years later about the year 1947 in Western and Central Europe. We identified the length of about 28–30 years of the dry cycles in Europe. In Eastern Europe are the peaks of the wet and dry cycles shifted by a few years compared to Northern and Western Europe. Generally we can state that the trend analysis did not show any important trends in selected European runoff series during the last 150 years.

**Keywords:** discharge, Europe, time series analysis, Hodrick-Prescott filter, long-term trends

## VORKOMMEN VON TROCKENEN PERIODEN IN DEN EUROPÄISCHEN ABFLUSSREIHEN

**Zusammenfassung:** Die niedrige Abflüsse der Flüsse Zentraleuropas während der letzten Jahren haben die Frage hervorgerufen, ob es auch in der Vergangenheit zu ähnlichen Abflußverhältnissen kam, oder ob es etwas außergewöhnliches bedeutet. Zweck des ersten Teiles dieses Beitrages ist das Vorkommen von den Trocken – und Naßperioden in der Danauabflußserie zu analysieren, und zwar entlang der ganzen Flußstrecke. Für die langfristige Analyse der Variabilität, der mittlere Jahresabfluß von 7 Pegelstellen entlang der Donau wurde benutzt. Die nässeste Dekade im Pegel Orsova war die 1910 – 1919, und die trockenste war 1857 – 1866. In dem Beitrag sind auch einige Methoden für die Identifizierung der langjährigen Trenden in den hydrologischen Zeitreihen präsentiert. Im Unterschied von klassischen Methoden (wie z.B. die der gleitenden Mittelwerte), im Beitrag konzentrieren wir in Detail auf den Hodrick – Prescott (HP) Filter.

In dem zweiten Teil des Beitrages sind die Trockenperioden der 17 anderen wichtigen Flüsse Europas analysiert. Auf Grund der ursprünglichen Abflußreihen wurden standardisierten Abflußreihen entwickelt, für die Gebiete West-, Ost-, Zentral-, und Nordeuropa. Für die Feststellung der langjährigen Abflußtrende des standardisierten Jahresabflusses benutzten wir den Hodrick – Prescott (HP) Filter. Die statistische Analyse zeigt, dass in diesen Zeitreihen lässt sich kein Trend (weder steigend noch sinkend) während der letzten 150 Jahren feststellen. Es lassen sich nur Trocken- und Naßperioden von verschiedener Dauer zu identifizieren. Außerordentlich trockene

Perioden kamen herum den Jahren 1863 und 1947 vor, und zwar in West- wie auch in Zentraleuropa. Wie stellten auch die Länge der Zyklen der Trockenperioden als um 28 – 30 Jahren fest. In Osteuropa sind die Scheitel der trockenen und nassen Zyklen um einige Jahren verschoben im Vergleich mit jenem in Nord- und Westeuropa. Im allgemeinen kann man sagen daß die Trendanalyse hat keine bedeutende Trends während der letzten 150 Jahren in den ausgewählten Abflußreihen Europas bestätigt.

**Schlüsselwörter** : Abfluß, Europa, Datenreihenanalyse, Hodrick – Prescott Filter.

## Introduction

Detection of the changes in river discharge trends is the most important and (at the same time) the most complicated step of water amount prognosis. Statistical analysis of the runoff oscillations depends on availability of long-term data series.

Systematic measurements of runoff in modern era started relatively late. The longest time series are available in Europe, but they do not exceed 200 years (Goeta (since 1807), Rhine (1808), Neman (1812), Dnieper (1818), Wesser (1821), Danube (1840), Vuoksa (1847), Elbe (1851), Neva (1859), Loire (1863), ...).

The longest available time series of mean annual runoff of the selected European largest rivers were used to analyse the long-term runoff trends.

In the first part of the paper, the occurrence of the dry periods in Danube River basin is analysed. The trend analysis of discharge time series of selected European main rivers is discussed in the second part of the study.

The annual runoff data series of European continent were obtained from following data sources:

- i) Global Runoff Data Center in Koblenz, Germany;
- ii) CD-ROM World Freshwater Resources prepared by I. A. Shiklomanov in the framework of the International Hydrological Programme (IHP) of UNESCO.

Runoff series fluctuations have their natural origin. Apart from it river discharge may have changed due to a range of human activities. Dams and artificial reservoirs dramatically change the natural flow regime. Currently the problems of the long-term runoff variability were discussed with respect to climate change. A number of studies was published all over the world. E.g., a special section of Hydrological Science Journal in February 2004 dealt with the issue of detecting changes in hydrological data. Authors Kundzewicz and Robson (2004), Sheng and Pilon (2004), Xiong and Guo (2004), Callède et al. (2004) focused on detecting changes in hydrological long time series. In Radziejewski and Kundzewicz (2004) a new concept of visualisation of the comprehensive change detection is demonstrated. In Burn et al. (2004) the trends in the Liard River (northern Canada) were investigated using Mann-Kendall test. They showed that the observed trends are related to both, trends in meteorological data and a large-scale oceanic and atmospheric process. In Slovakia, Hlavcova et al. (1999) studied the possible impact of climate change upon runoff regime and analysed the unfavourable decreasing runoff trend in 1981–1995. Kostka and Holko (2000) studied the impact of climate changes to hydrological regime in small mountainous basin, and Halmova (2000) analysed the water storage in reservoirs. Pekarova and Miklanek (2004) analysed long-term course of 27 discharge series from the database of National Climate Programme SR (period 1930–2000). Regardless the fact that they showed the decrease of discharge in South Slovakia in decade 1982–1993, they emphasize from the long term point of view the necessity to identify hidden periods in the long-term series. As mentioned in Pekarova (2003) and Pekarova et al. (2003), it is necessary to come out from sufficiently long time discharge series, because of possible confusion between trend and cyclicity. Therefore, in the first step of discharge series analysis, we have to separate hidden cycles from long-term trend.

## 1. Methods

The basic methods for the long-term trend identification are:

- Exploratory data analysis

- Tests for step change (for example Wilcoxon-Mann-Whitney test, Distribution-free CUSUM test, Kruskal-Wallis test, ...)
- Tests for trend (Sperman's  $\rho$  test, Kendall's  $\tau$  test, ...)

The general guidance to the methodology of the change detection in the hydrological time series can be found in Prochazka et al. (2001).

Generally, the most common assumptions in change point hypothesis testing are normality (population is distributed normally) and statistical independence (randomness) of observations.

1. Therefore, in the first step we test, whether the discharge time series  $x_t$  is distributed normally. In the case the series is not of normal distribution, we use appropriate transformation and work on with transformed time series  $y_t$ .
2. Then we test the covariance structure of the series  $y_t$ : we look for hidden periods, trend, and autoregressive and moving average component of the series.
  - a) We search hidden periods by periodogram with Fisher's test or by combined periodogram method (Pekarova et al. 2003). In the case the hidden periods were found in the time series, we try to remove the harmonic (deterministic) component from the time series;
  - b) We test long-term trend with Sperman's  $\rho$  test, or Kendall's  $\tau$  test, ...;
  - c) To remove the trend component (linear, quadratic), autoregressive component, and moving average component from the time series we search for the appropriate Box-Jenkins ARIMA model (autocorrelation function, partial autocorrelation function). We have to test the correctness of the ARIMA model specification (the autoregressive part of the B.-J. model must be stationary, the moving average part must be invertible, and residuals/innovations must be Gaussian white noise).

When significant periods  $\lambda_j$ , long-term trend, and autocorrelation component in the series are found, it is possible to describe the discharge time series  $y_t$  by the model of the following general form:

$$y_t = A_0 + \sum_{j=1}^m \left( \underbrace{A_j \cos(\lambda_j t) + B_j \sin(\lambda_j t)}_{\text{a harmonic component}} \right) + \underbrace{ARIMA}_{\text{an ARIMA component}} + z_t, \quad t = 1, \dots, N. \quad (1)$$

where:

- $y_t$  - the transformed average annual discharge;
- $\lambda_j$  - the significant frequencies given by the periodogram;
- $A_j, B_j, j = 1, 2, \dots, m$  - parameters of the harmonic component ( $A_0$  – the mean of the time series);
- $ARIMA$  - the autoregressive component, a.k.a. Box-Jenkins model;
- $z_t$  - the adjusted time series, residuals.

This model can be used for the long-term annual discharge prediction (Lohre et al.).

### 1.1. Hodrick-Prescott filter

To identify long term trends in this study we used the Hodrick-Prescott filter (HP filter) (Maravall, 2001). Hodrick-Prescott filter decomposes given time series to a trend as well as a cyclical component. Asset of HP-filter is, (compared to moving average technique) the values of trends are calculated as well as for the end values of the series, that is great advantage for the prognoses of discharge in the future.

Assume we are interested in decomposing a time series of yearly discharge

$$\{x_i\}_{i=1}^n \text{ into a long-term trend } Tr_i \text{ and a residual, } C_i. \text{ The HP filter provides the sequences } \{Tr_i\}_{i=1}^n \text{ and } \{C_i\}_{i=1}^n \text{ such that:}$$

$$x_i = Tr_i + C_i \quad i=1, \dots, n, \quad (2)$$

and the loss function

$$\sum_{i=1}^n C_i^2 + \alpha \sum_{i=3}^n (\nabla^2 Tr_i)^2 \quad (3)$$

(where:  $\nabla^2 Tr_i = Tr_i - 2 \cdot Tr_{i-1} + Tr_{i-2}$ )

is minimized.

The first term in (3) penalizes large residuals (i.e. poor fit), while the second term penalizes lack of smoothness in trend. The parameter  $\alpha$  regulates the trade-off between the two criteria.

### 1.2. Occurrence of the dry periods in Danube river basin

We assembled the mean annual runoff series of seven stations along the Danube River from the GRDC (Global Runoff Data Center, Koblenz) database with the aim to analyse the long-term variability of the mean annual runoff along the Danube River: 1. Hofkirchen; 2. Achleiten; 3. Kienstock (till 1970 Stein - Krems); 4. Bratislava; 5. Nagymaros; 6. Turnu Severin (till 1970 Orsova); 7. Ceatal Izmail.

The wet and dry periods as well as the long-term trends are easy to show on the plots of the filtered values. In Fig. 1 is the plot of double 5-year moving averages of the Danube discharge in seven stations and at the mouth. The wet and dry periods are easy to be identified at the graph. The course of the individual periods is identical along the whole river stretch.

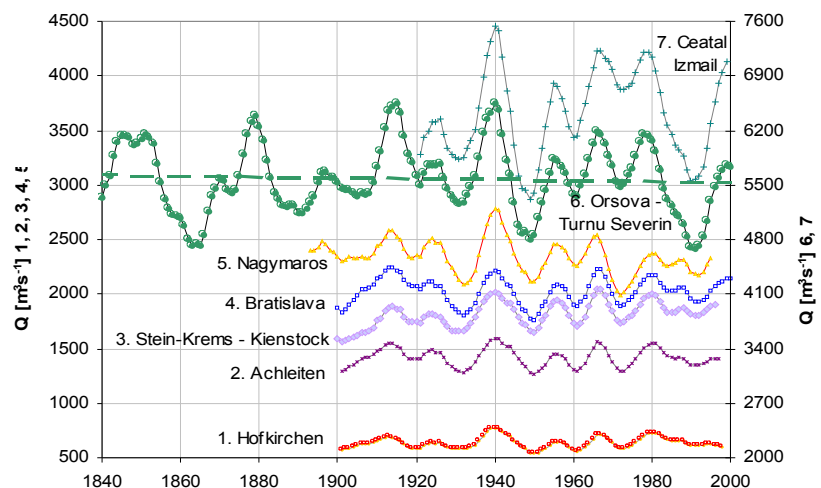


Figure 1. The double 5-year moving averages of discharge in seven Danube stations along the river.

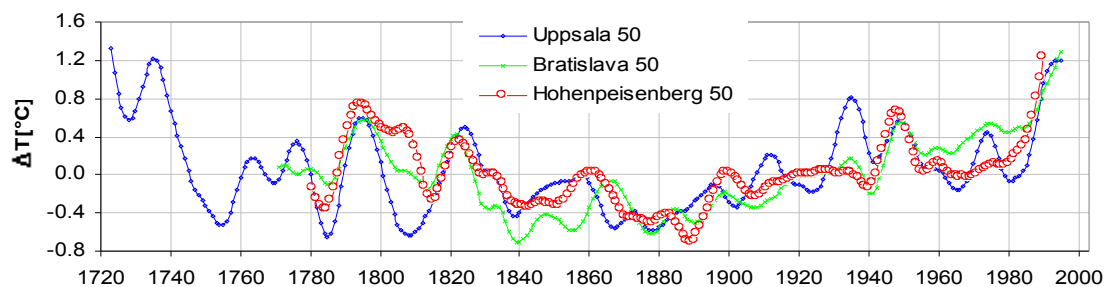


Figure 2. Courses of the filtered annual air temperature (HP filter for  $\alpha = 50$ ), deviation from the long-term mean. Hohenpeissenberg, Uppsala (Moberg, Bengström, 1997) and Bratislava stations (Konček, 1972), 1720–1995 period.

The data from the station Turnu Severin are very important for the trend analysis, as they are collected in a rocky profile since 1840 and we can trust them. The minimum

annual discharge in Orsova (today Turnu Severin) was in 1863,  $Q_{\min} = 3471 \text{ m}^3\text{s}^{-1}$ , while the maximum one was in 1915,  $Q_{\max} = 8265 \text{ m}^3\text{s}^{-1}$ . The analysis of the Orsova data shows that the wettest decade was in 1910–1919, while the driest one was in 1857–1866, when the global maximum and minimum annual discharge was observed, respectively.

These results indicate that the period around the year 1862 was the driest period in the Central Europe since 1840. It is interesting to notice that in the period around the year 1862 was the mean annual air temperature in Europe lower by about  $0.8^\circ\text{C}$  compared to the 1990s` (see Fig. 2).

Two of the driest periods of the instrumental era occurred in very different temperature conditions. It shows that the mean annual air temperature does not have direct influence on the runoff depth and the long-term runoff variability has its own dynamics. Therefore we cannot automatically suppose, that the expected increase of the air temperature will result in decrease of runoff in Danube River.

## 2. Occurrence of the dry periods in European runoff series

Our aim is to find if and when the dry periods occurred in other European runoff series. The longest runoff records are available in Europe and therefore they are suitable for the identification of the long-term trends. We analysed more than 30 runoff series of the main European rivers. We used Hodrick - Prescott filter for visual identification of the cyclic component with parameter  $\alpha=10, 50, 400, \text{ and } 1600$  (Pekarova and Pekar, 2002). The results of the filter application on mean annual runoff series of Danube in Turnu Severin, Rhine in Cologne, Göta and Neva rivers for  $\alpha = 10, 50, 400, \text{ and } 1600$  are in Figs. 3a-d.

On Fig. 3a we can identify significant dry periods 1861–1865; 1945–1948, and 1988–1993 on Danube. According to Lindström and Bergström (2004), the beginning of the seventies in last century (period 1972–1976) was extremely dry in Sweden (see Fig. 3c), and the end of the 20<sup>th</sup> century was above average wet (unlike the central Europe). Dry periods were recorded in Göta runoff series in 1855–1860 and 1940–1945, too.

The 29-year cycle of runoff variability can be clearly identified in the Neva river series. The Neva river drains the territory of the Finnish and Russian lakes which accumulate large volume of water, and thus multiannually regulate and smooth the runoff. The Neva runoff records are processed since 1859, therefore the dry period around 1858 is not recorded. It is possible to prolong the Neva runoff series by regression to the Finnish river Vuoksa having the records from 1847. The driest year on Neva was in 1940 with the mean discharge of  $1340 \text{ m}^3\text{s}^{-1}$ , the wettest one was 1924 with the mean discharge of  $3670 \text{ m}^3\text{s}^{-1}$ . The driest period on Neva occurred in 1939–1942, by about 7 years earlier than in the Danube basin. At the same time we should notice that the period 1939–1942 was quite wet in the Danube basin. Such analysis supports the hypothesis, that the dry periods do not occur in European rivers simultaneously, but they are a few years shifted depending on location of the basins.

The time lag of the dry periods between Danube and Neva runoff is shown on Fig. 4. The mean time lag is about 11-12 years. Typically, the dry periods in the Danube basin were accompanied by the wet periods in the Neva basin in the 20<sup>th</sup> century.

It follows from the analysis that we did not find long-term continuous decrease or increase of the runoff. We can identify the dry and wet periods in river runoff series. In case of the cyclic series (and hydrological series are such) we cannot express the trend simply by the linear function and to expect the continuation of the linear development in the future. If we want to apply the linear trend function, we must relate it to specific period. E.g. the linear trend of Rhine runoff was decreasing in 1870–1950, and increasing in 1945–1985.

In the next paragraphs we will try to compile one runoff series representing the runoff from Europe and to identify the long-term trend in such series.

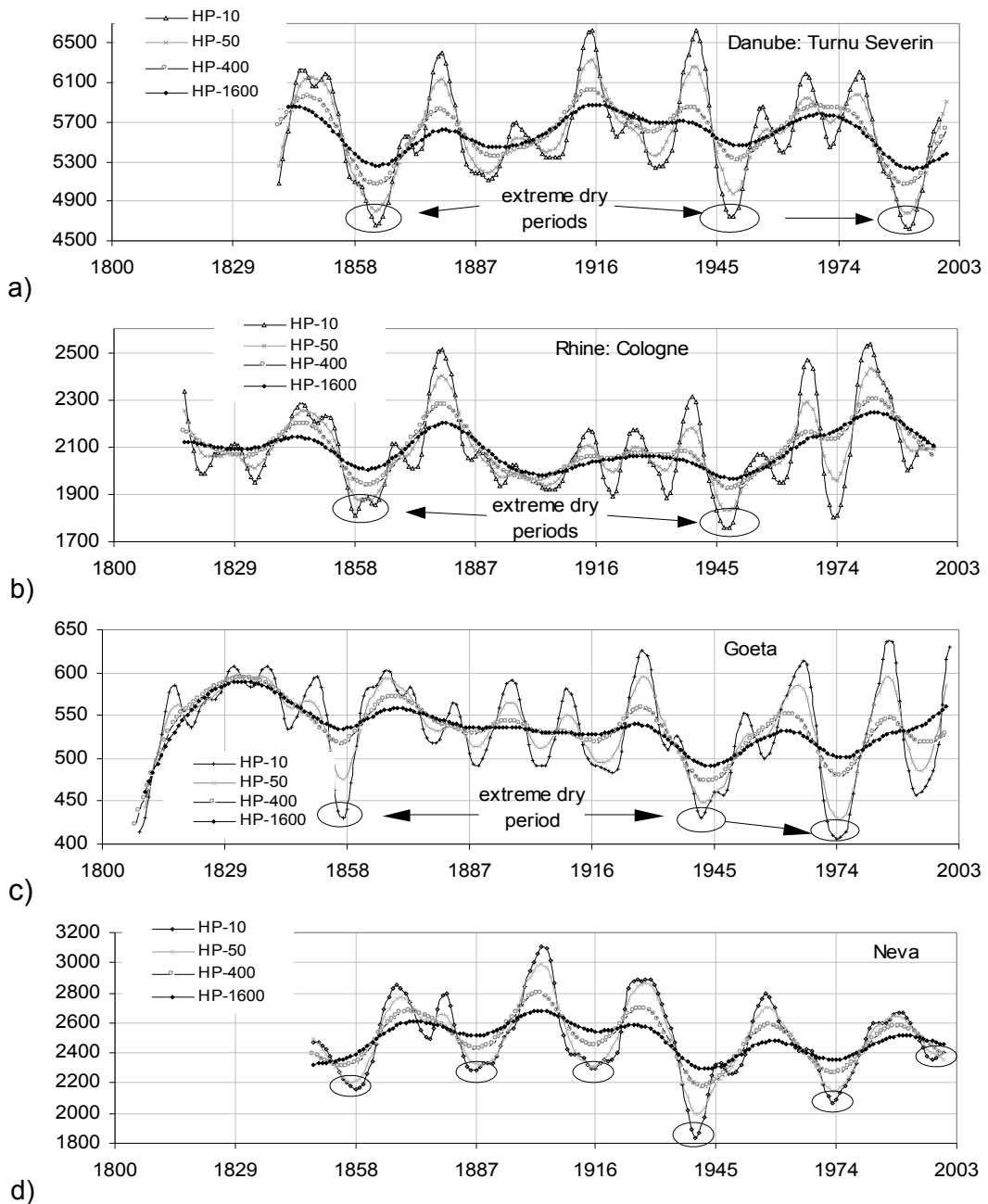


Fig.3 Course of the filtered annual mean discharge in  $[m^3s^{-1}]$ , HP filter for  $\alpha = 10, 50, 1600, 6400$ . Identification of dry and wet period, as well as of long - term trend.  
a) Danube at Turnu Severin, period 1840–2000; b) Rhine at Cologne, period 1808–1998; c) Göta, period 1808–2002; d) Neva, period 1859–2000.

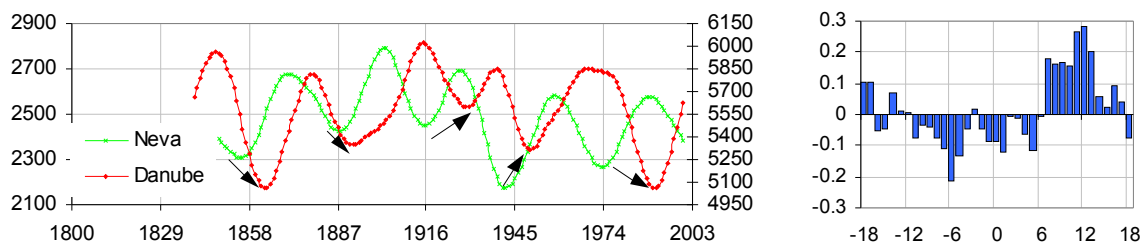


Figure 4. Course of filtered annual discharge  $[m^3s^{-1}]$  HP-filter for  $\alpha = 400$ , Danube and Neva. Lag of dry periods – left. Cross-correlations between Danube and Neva discharge (raw data) - right.

## 2.1. Long term trend of European discharge series

In order to identify trends for some European rivers, discharge time series of eleven rivers for West/Central Europe were used (Rhine: Cologne, DE (1816–1997), Neman: Smalininkai, LT (1912–1993), Loire: Montjean, FR (1863–1986) Wesser: Hann-Muenden, DE (1831–1994), Danube, Turnu Severin, RO (1840–1988), Elbe: Decin, CZ, (1851–1998), Oder: Gozdowice, PL (1900–1993), Vistula: Tczew, PL (1900–1994), Thames: Kingston, GB (1881–2000), Rhone: mouth, FR (1921–1986), and Po: Pontelagoscuro, IT (1918–1979)). Three time series for East Europe were used (Dniepr: Locmanskaja Kamjanka, UA (1818–1984), Don: Razdorskaya, RU (1891–1984), and Volga: mouth, RU (1882–1998)). For North Europe four time series were used (Neva: Novosaratovka, RU (1859–1984), N. Dvina: Ust-Pinega, RU (1881–1990), Goeta: Vaenersborg, SE (1807–1992), Pechora: mouth, RU (1921–1987)). Location of selected rivers is sketched on Figure 5, basic hydrological characteristics are presented in Table 1. These data series were completed by the multiple regression methods (period 1850–1997) and the standardised average discharge time series was computed.

From the point of view of the annual discharge, the driest year during the period 1850–1997 was the year 1921. The extremely wet years were 1926 as well as 1941 (see Fig. 6 and 8a). Correlation matrix of the 17 selected discharge time series are presented in Table 2. From the values of the correlation coefficients (and from the previous analysis) follows negative correlation between discharge series of north-east European rivers and south-west European rivers – dry periods have a time lag.

The course of the filtered standardised discharge data by HP filter of the West European time series are given in Fig. 7a, of East Europe in Fig. 7b, and of Europe in Fig. 7c.

Finally, the representative standardised discharge time series of the whole Europe from the 18-discharge series was constructed (Fig. 8a) for the period 1850–1997 (annual discharge of 18 series were summed up and then standardised). Extreme values from the years 1921 and 1926 (minimum and maximum) influenced the course of 10-years moving averages of coefficients of variation as well as symmetry (Fig. 8b).

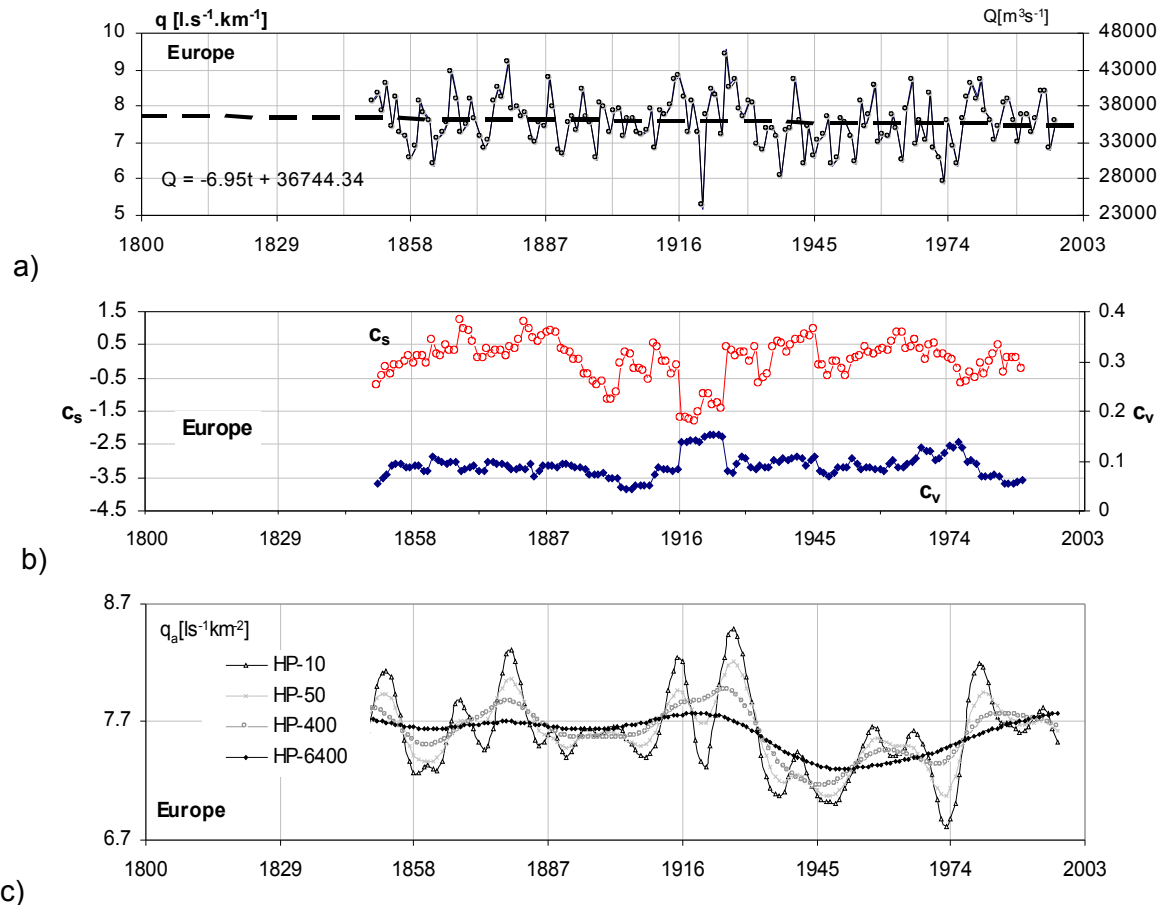
Figure 5. Locations of the selected European rivers.











**Figure 8.** Course of the representative discharge series of Europe (1850–1997).  
 a) Annual specific yield [ $l \cdot s^{-1} \cdot km^2$ ] (or average annual discharge [ $m^3 \cdot s^{-1}$ ]).  
 b) Course of 10-years moving average of coefficients of variation and symmetry.  
 c) Filtered annual specific yield [ $l \cdot s^{-1} \cdot km^2$ ], HP - filter.

The dry period occurred in Europe around 1835 and the years 1857–1862 were very dry. In the 20<sup>th</sup> century the period 1946–1948 was the driest. Another dry period occurred in 1975.

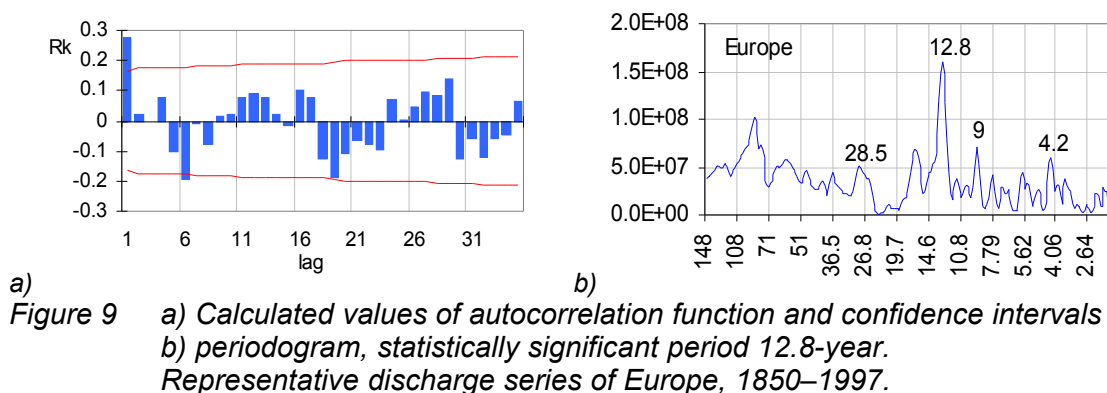
If we want to identify any trend uninfluenced by the periodicity of the discharge time series, we must determine the trend during a closed multiple loop, starting and terminating by either minima (e.g., 1861–1946 in Central Europe) or maxima (e.g., 1847–1930 or 1931–1984 in Central Europe). Trends determined for other periods are influenced by the periodicity of the series and depend on the position of the starting point on the increasing or recession curve.

The other way is to remove the cyclical component from the discharge series and test the adjusted series  $z_t$  (see eq (1)).

According the tests of normality it follows, that the discharge series of whole Europe is normally distributed. Using the test Number of runs we can reject on the significance level 0.05 the hypothesis  $H_0$ , that the representative discharge series from the whole Europe is independent. The test detected a periodical change in this series.

On the Figure 9a, calculated values of autocorrelation function and confidence intervals of the representative discharge series (1850–1997) are presented. There exist statistically significant negative dependence of the discharge on the value six years ago. As you can see on Figure 9b from the combined periodogram, statistically significant period has 12.8-year duration.

The trend analysis does not show any significant linear trend change in long-term discharge series (1850–1997) in representative European discharge series. If we consider the 28-29-year cycle, we can expect the next wet period in Central Europe to occur in next years (around 2009).



### 3. Conclusions

In the presented study, the long-term trends and cyclicity in hydrological time series are identified using the Hodrick-Prescott (HP) filter. The HP filter seems to be a good tool for analysing annual time series. It clearly identifies the fluctuation in discharge time series.

The results indicate that the period around the year 1862 was very dry period in the Danube River. It is interesting to notice that in the period around the year 1862 was the mean annual air temperature in Europe lower by about 0.8°C compared to the 1990s. Two of the driest periods of the instrumental era (around 1862 and 1990) occurred in very different temperature conditions. This shows that the mean annual air temperature does not have direct influence on the runoff depth and the long-term runoff variability has its own dynamics. Therefore we cannot automatically suppose, that the expected increase of the air temperature will result in decrease of runoff in Danube River.

In the Western Europe, the extremely dry periods were around the year 1863 and 86 years later around the year 1947. The runoff extremes (in both dry and wet periods) in the Eastern Europe precede by 3-5 years the peaks in the Western Europe. The time lag is increasing with the distance of the basins.

According to the Figs. 5a-c we can estimate the length of the cycles of dry periods as 28–30 years in both Western-Central and Eastern Europe regions.

Generally we can comment that the trend analysis did not show any significant trends in cumulative runoff series of the major European rivers in last 150 years.

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